

Development of Reliability-Based Damage Tolerant Structural Design Methodology

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July 21, 2009



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FAA Sponsored Project Information



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- **FAA Technical Monitor:** Dr. Lynn A. Stulen, FAA AF 2000-1-1-1

- **Other FAA Personnel:** Dr. Lynn A. Stulen, FAA AF 2000-1-1-1

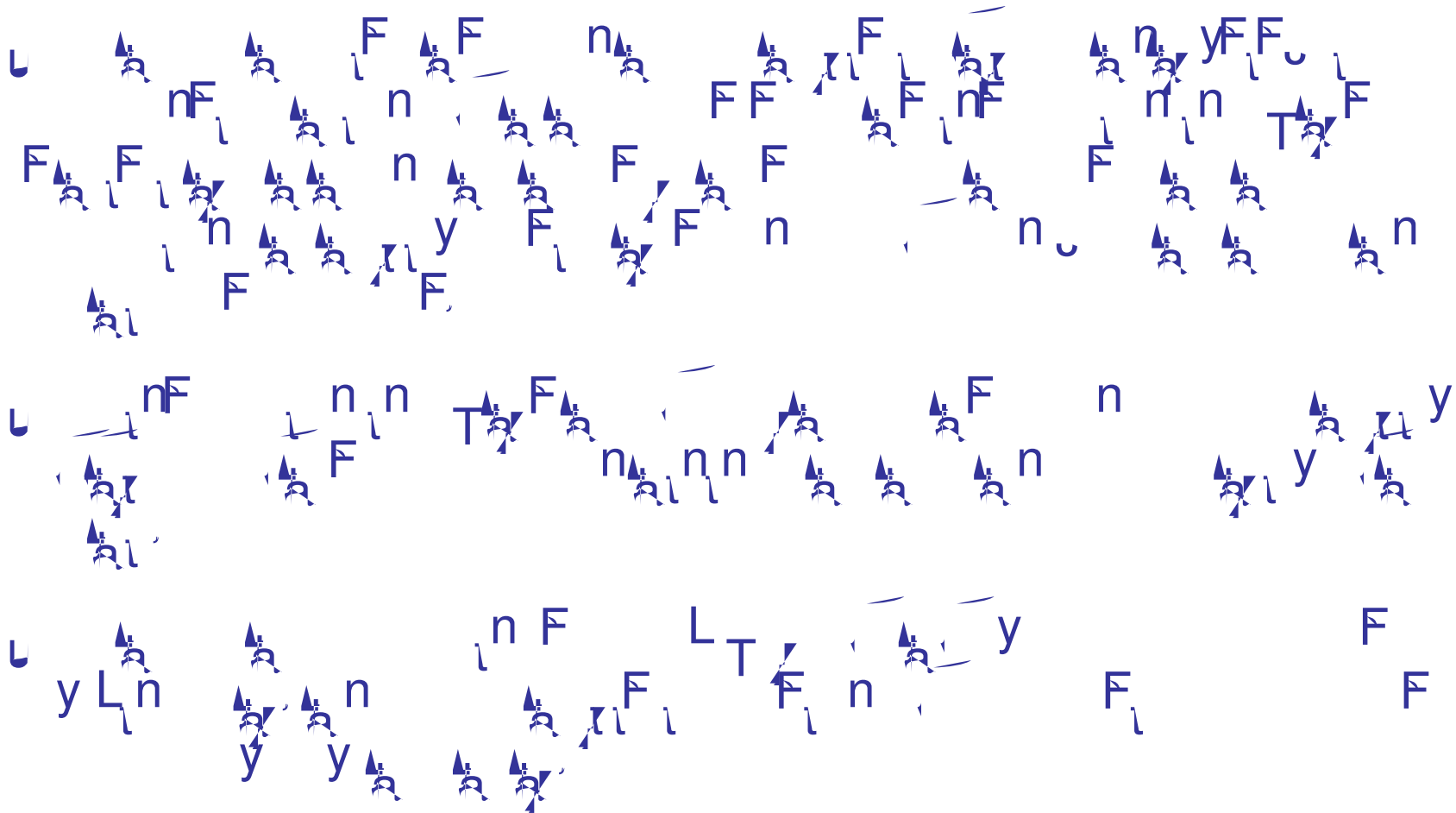
- **Industry Participants:** Dr. Lynn A. Stulen, FAA AF 2000-1-1-1

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- **Industry Sponsors:** Dr. Lynn A. Stulen, FAA AF 2000-1-1-1



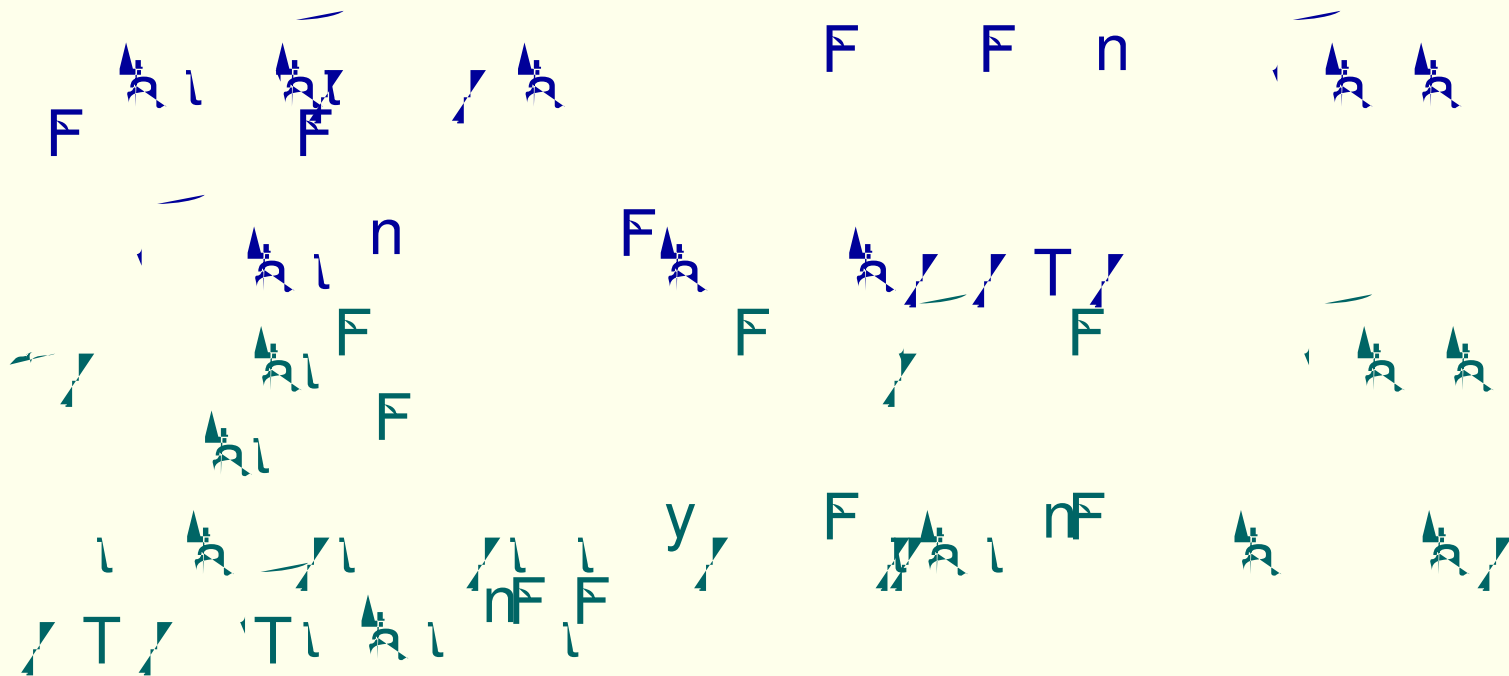
Technical Approach



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Program Capabilities: Various Failure Modes



**See the FAA Grant "Combined Local-Global Variability and Uncertainty in the Aeroservoelasticity of Composite Aircraft"*



Analysis of Disbond/Delamination Arrest Mechanisms





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Model Description



$$C = \frac{t_1 + t}{d} \cdot \frac{b}{n} \cdot \frac{1}{t_1 E_1} \cdot \frac{1}{nt E} \cdot \frac{1}{nt_1 E_3} \cdot \frac{1}{nt E_3}$$

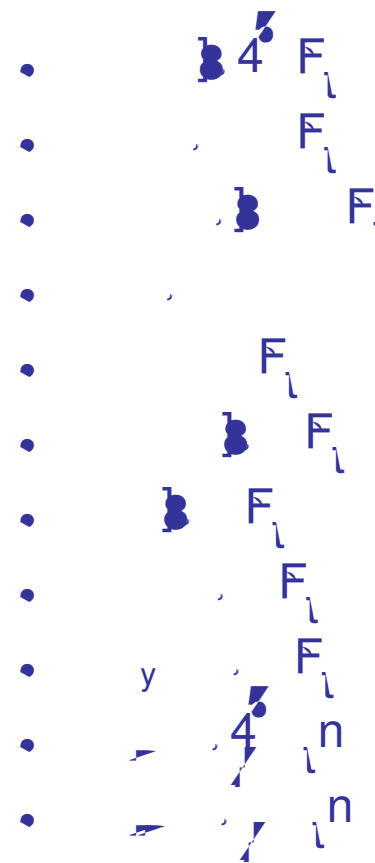
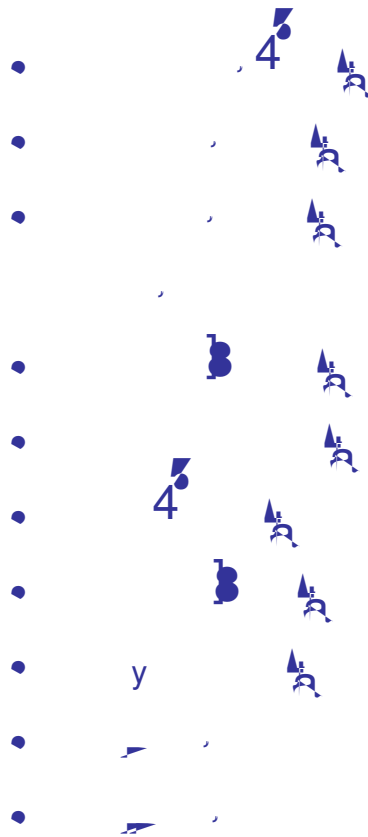


Model Description





Material Properties (AS4/3501-6)





Laminate Configuration (16 plies)



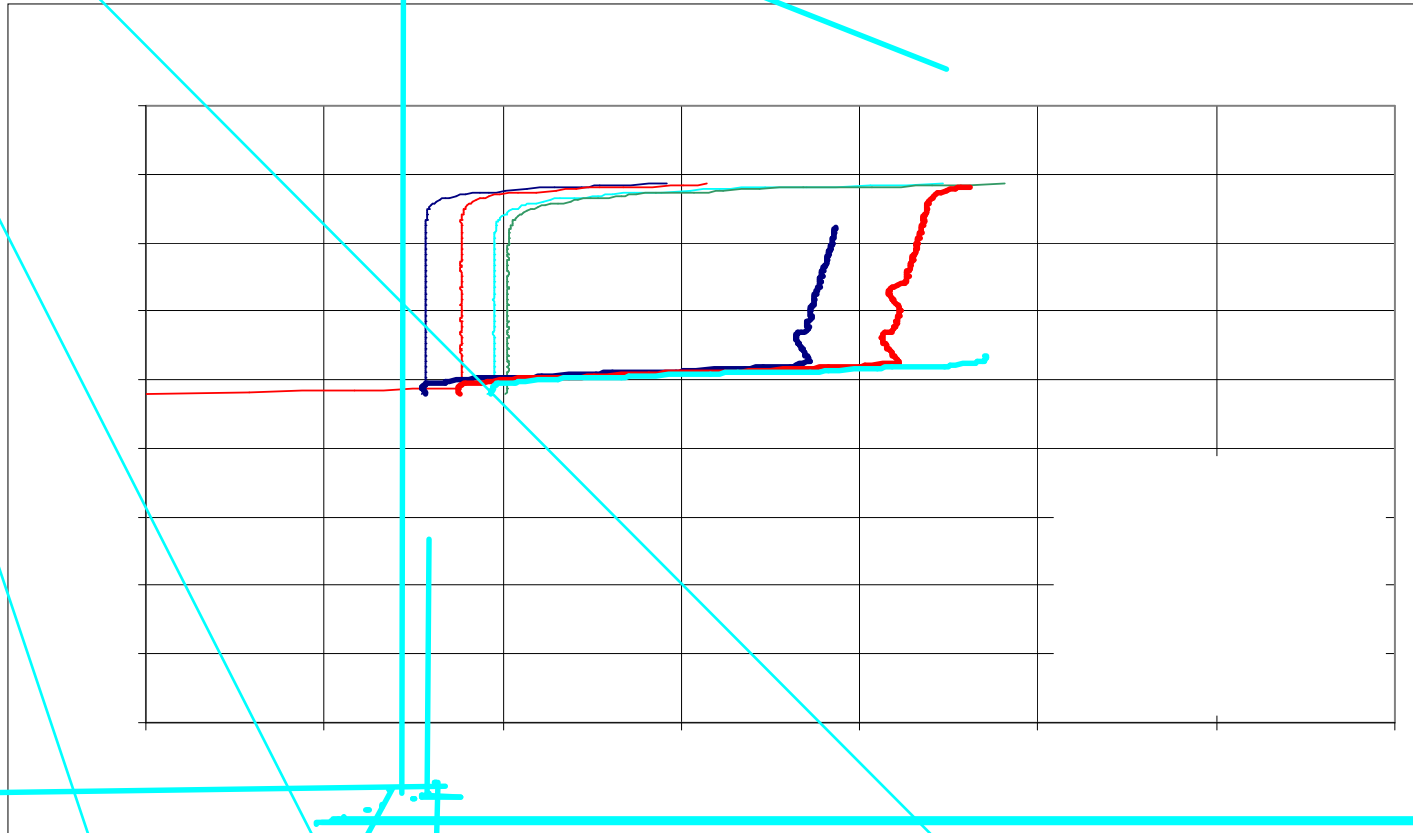
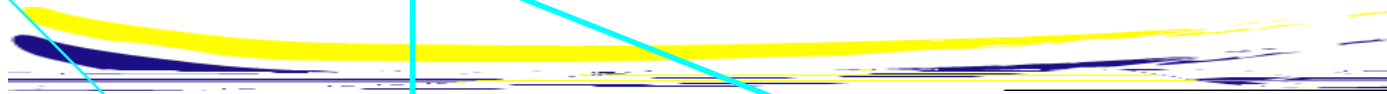
0-ply	Lay-up	E_x	C (in/lb)
4_1	$4_1 4_1 4_1 4_1 F$, "	, "
, 4_1	$4_1 4_1 4_1 4_1 F$, "	, 4_1 "
4_1 ,	$4_1 4_1 F$, "	$4_1 4_1$,
, 4_1	$4_1 4_1 F$, "	$4_1 4_1$,

$$C = \frac{t_1 + t}{d} \frac{a}{n} \frac{1}{t_1 E_1} + \frac{1}{nt E} + \frac{1}{nt_1 E_3} + \frac{1}{nt E_3}$$

$$a = 1/3, b = 1, n = 1$$

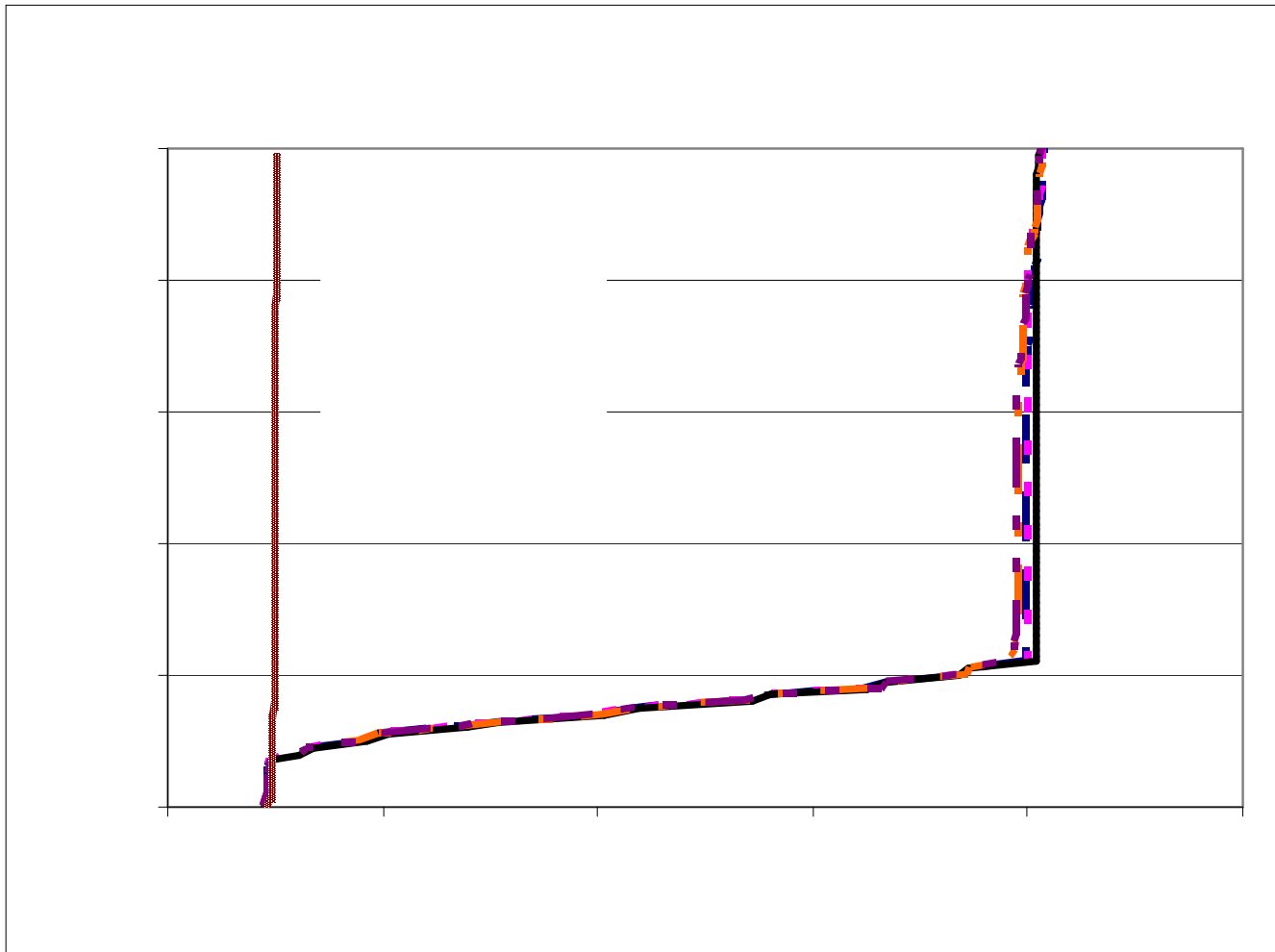
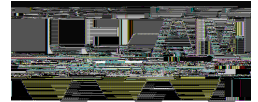


Results: Applied Moment M Only





Growth of a Disbond Caused by Applied Moment M



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Mode Decomposition: Applied Moment M Only

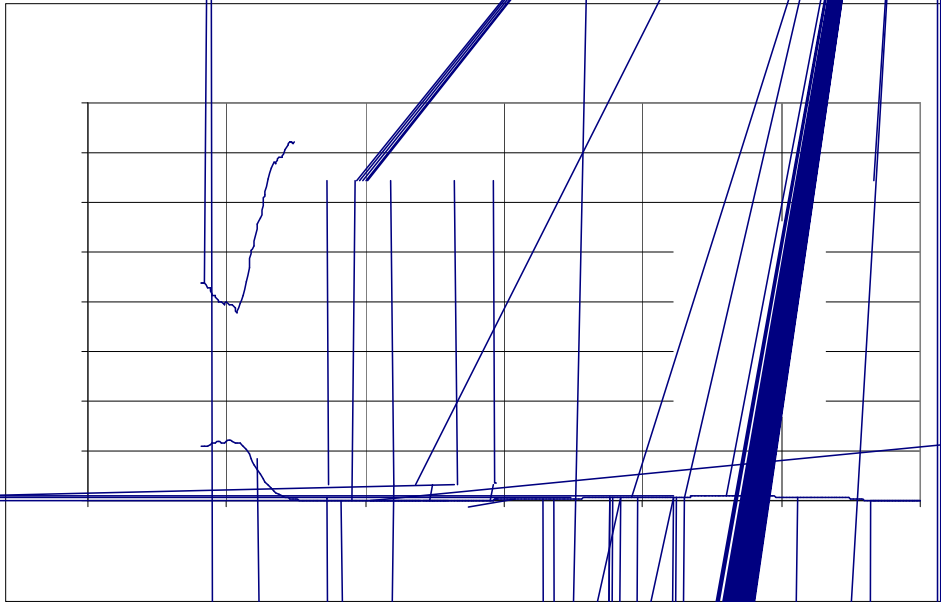
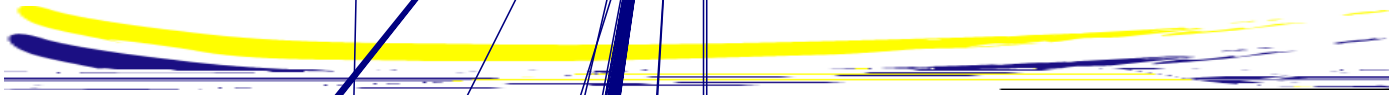






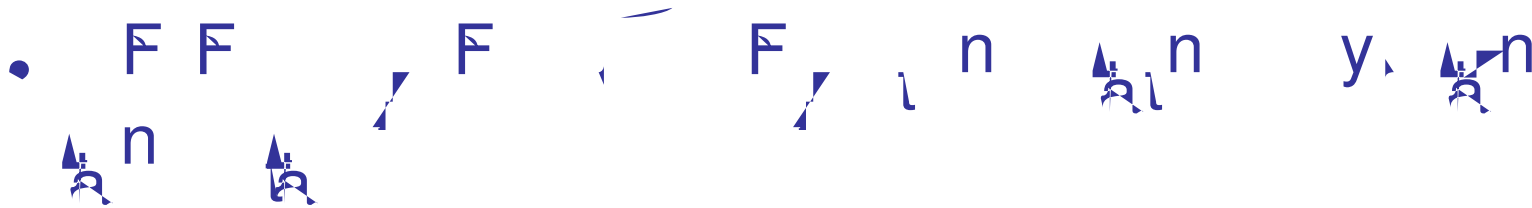


Mode Decomposition: Applied Tension N Only



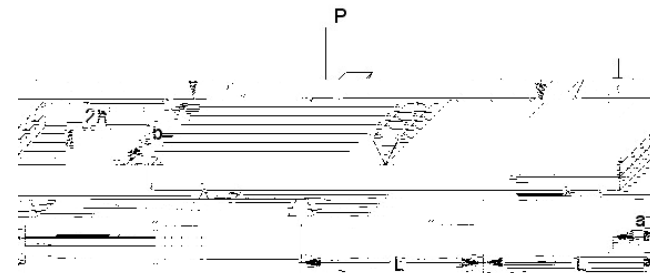
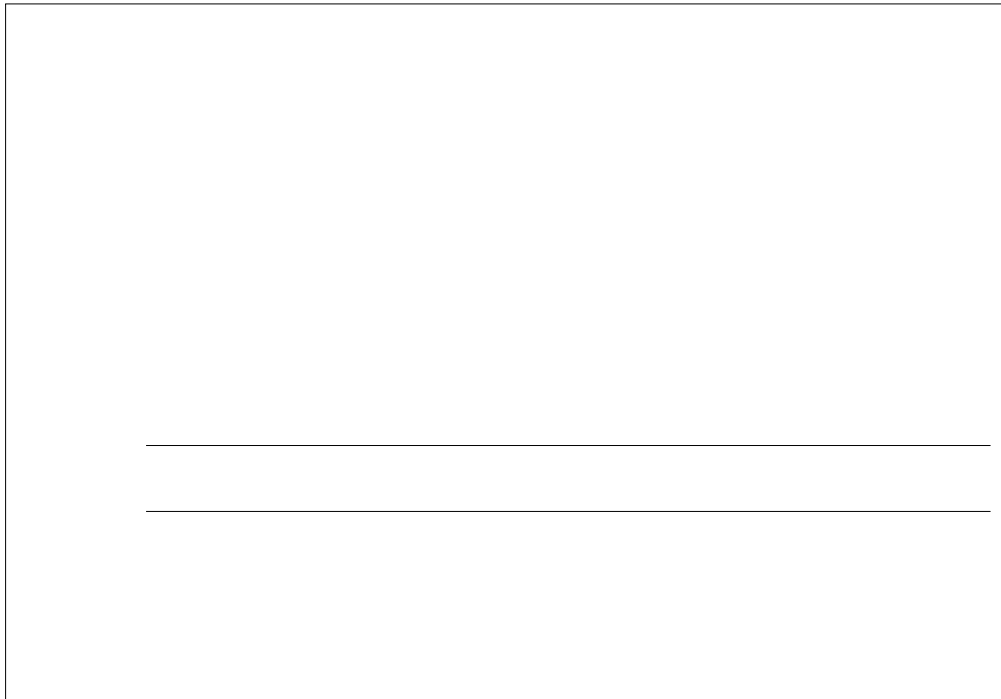


Crack-Tip Fracture Analysis



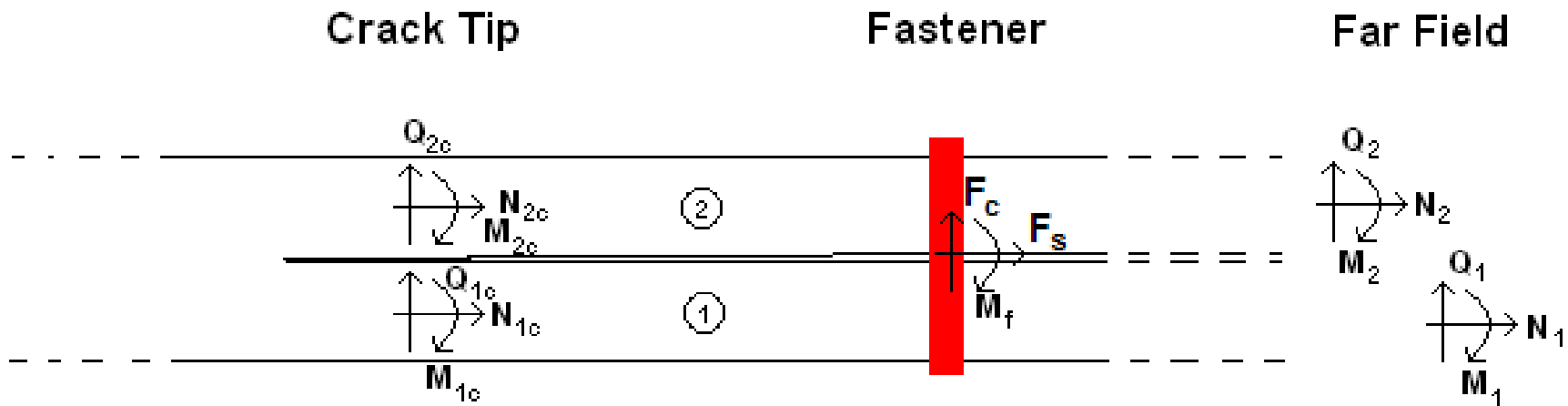


Comparison with Classical Beam Solutions





Local Crack-tip and Far-field Applied Forces and Moments



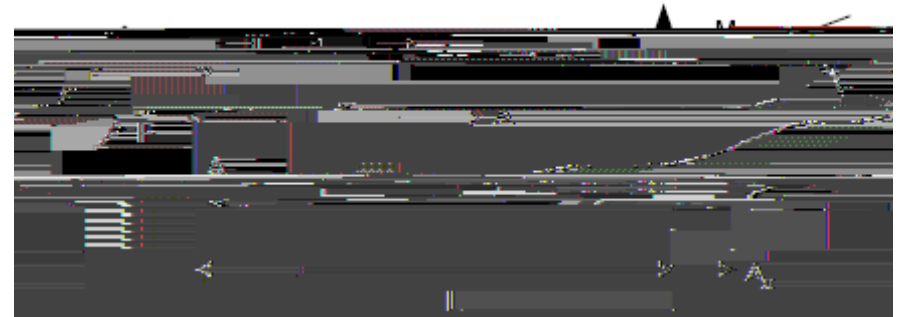




Nonlinear Beam Analysis



$$\frac{E}{I} \frac{M}{Y''}$$
$$\frac{1}{(1 - Y'')^3} \frac{1}{1}$$
$$\left(\begin{array}{c} \\ \\ \\ \end{array} \right) \quad \left(\begin{array}{c} x \\ \\ \\ \end{array} \right) \quad \left(\begin{array}{c} y \\ \\ \\ \end{array} \right)$$
$$'' \quad \left(\begin{array}{c} x \\ \\ \\ \end{array} \right) \quad \left(\begin{array}{c} y \\ \\ \\ \end{array} \right)$$





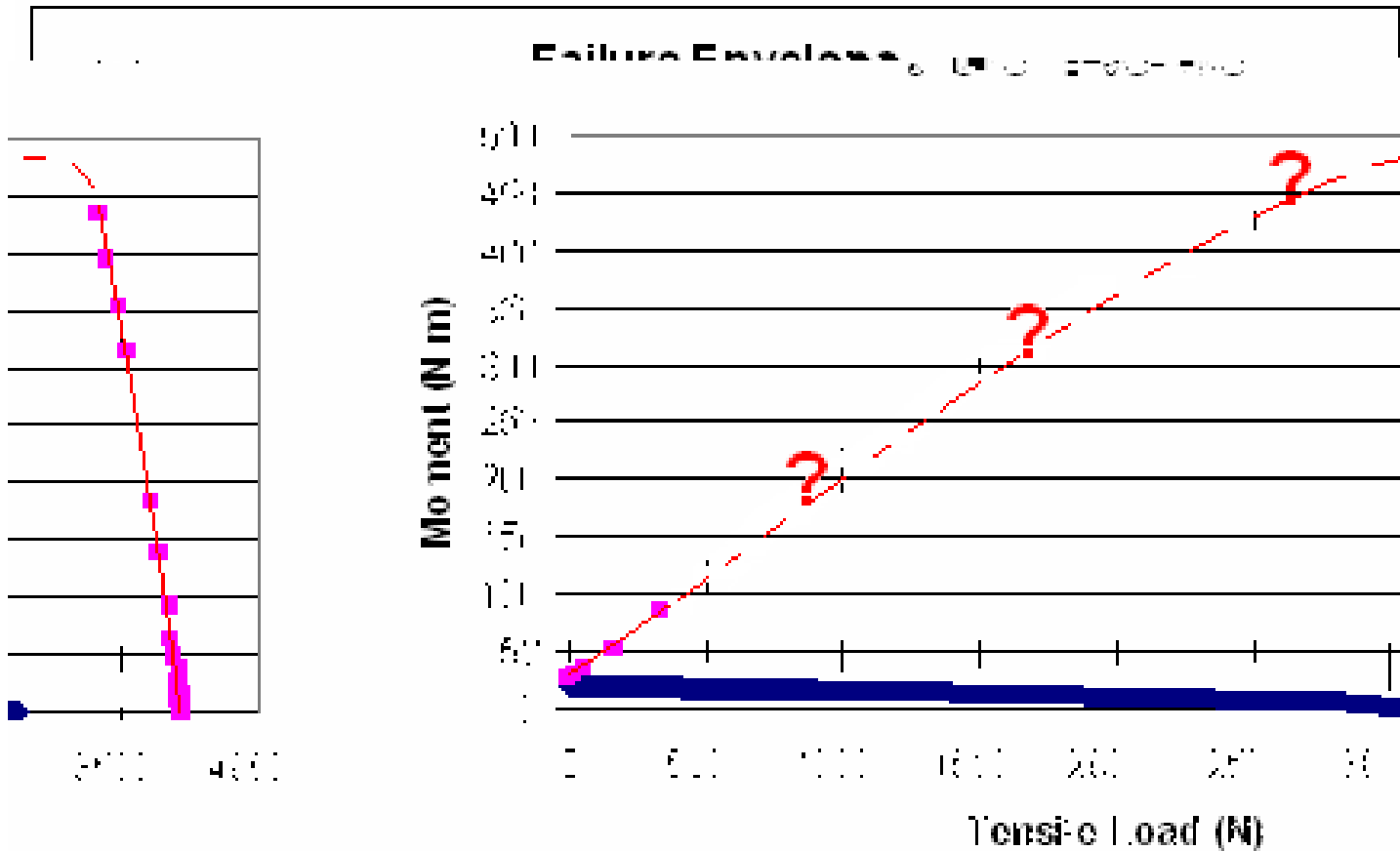
Comparison Between Linear and



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Failure Envelope Between N and M





Work in Progress / Future Work



- n A F n F
- T n y F F 4 n F
- n F n F n n n n 4 n n
- n n n n n n n n n n
- n F n F n F n n n n
- n y y T n F F n n n n
- F n T n n n n F

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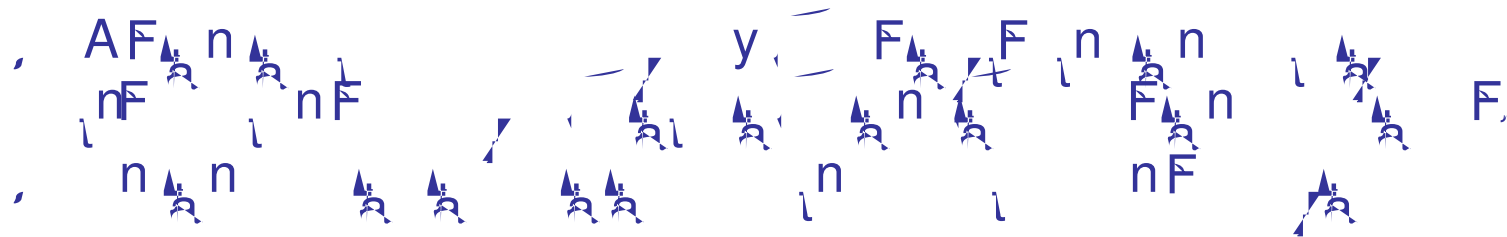
A Look Forward



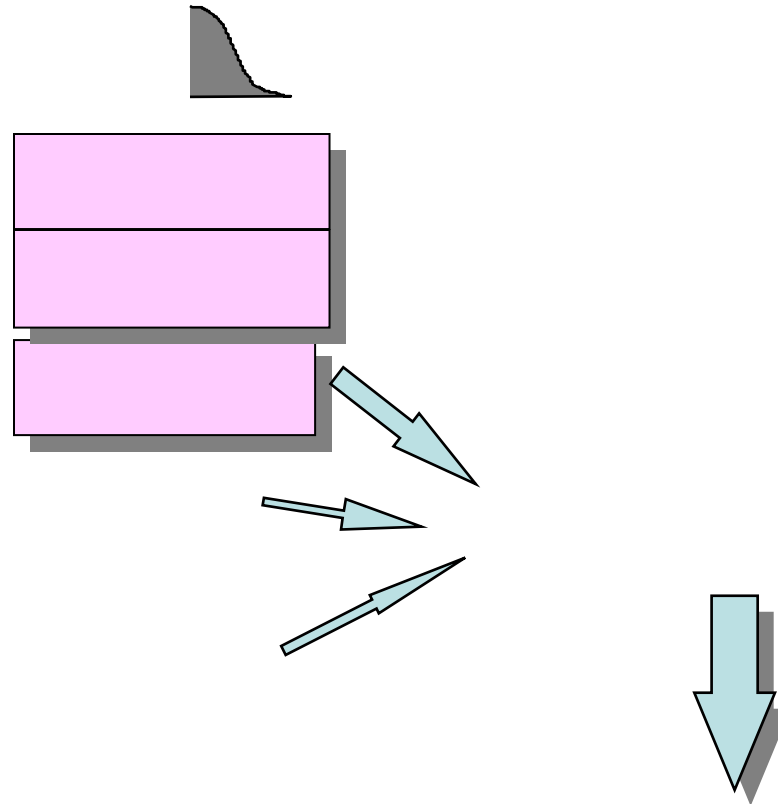
Benefit to Aviation



Future needs







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